Stage 8

N Number

Ni Integers, powers and roots

- 8Ni1 Add, subtract, multiply and divide integers
- **8Ni2** Identify and use multiples, factors, common factors, highest common factors, lowest common multiples and primes; write a number in terms of its prime factors, e.g. $500 = 2^2 \times 5^3$
- **8Ni3** Calculate squares, positive and negative square roots, cubes and cube roots; use the notation $\sqrt{49}$ and $\sqrt[3]{64}$ and index notation for positive integer powers

Np Place value, ordering and rounding

- 8Np1 Read and write positive integer powers of 10; multiply and divide integers and decimals by 0.1, 0.01
- **8Np2** Order decimals, including measurements, making use of the $=, \neq$, > and < signs
- **8Np3** Round whole numbers to a positive integer power of 10, e.g. 10, 100, 1000 or decimals to the nearest whole number or one or two decimal places

Nf Fractions, decimals, percentages, ratio and proportion

- 8Nf1 Find equivalent fractions, decimals and percentages by converting between them
- 8Nf2 Convert a fraction to a decimal using division; know that a recurring decimal is a fraction
- 8Nf3 Order fractions by writing with common denominators or dividing and converting to decimals
- **8Nf4** Add and subtract fractions and mixed numbers; calculate fractions of quantities (fraction answers); multiply and divide an integer by a fraction
- **8Nf5** Calculate and solve problems involving percentages of quantities and percentage increases or decreases; express one given number as a fraction or percentage of another
- 8Nf6 Use equivalent fractions, decimals and percentages to compare different quantities
- **8Nf7** Simplify ratios, including those expressed in different units; divide a quantity into more than two parts in a given ratio
- 8Nf8 Use the unitary method to solve simple problems involving ratio and direct proportion

Nc Calculation

Mental strategies

- **8Nc1** Use known facts to derive new facts, e.g. given $20 \times 38 = 760$, work out 21×38
- **8Nc2** Recall squares to 20 × 20, cubes to 5 × 5 × 5, and corresponding roots
- 8Nc3 Recall simple equivalent fractions, decimals and percentages
- 8Nc4 Use known facts and place value to multiply and divide simple fractions
- 8Nc5 Use known facts and place value to multiply and divide simple decimals, e.g. 0.07 × 9, 2.4 ÷ 3
- **8Nc6** Use known facts and place value to calculate simple fractions and percentages of quantities
- **8Nc7** Recall relationships between units of measurement
- 8Nc8 Solve simple word problems including direct proportion problems
- 8Nc9 Use the laws of arithmetic and inverse operations to simplify calculations with integers and fractions
- 8Nc10 Use the order of operations, including brackets, with more complex calculations

Addition and subtraction

• **8Nc11** Consolidate adding and subtracting integers and decimals, including numbers with differing numbers of decimal places

Multiplication and division

- **8Nc12** Divide integers and decimals by a single-digit number, continuing the division to a specified number of decimal places, e.g. 68 ÷ 7
- 8Nc13 Multiply and divide integers and decimals by decimals such as 0.6 or 0.06, understanding where to place the decimal point by considering equivalent calculations, e.g. 4.37 × 0.3 = (4.37 × 3) ÷ 10, 92.4 ÷ 0.06 = (92.4 × 100) ÷ 6

A Algebra

Ae Expressions, equations and formulae

- **8Ae1** Know that letters play different roles in equations, formulae and functions; know the meanings of *formula* and *function*
- **8Ae2** Know that algebraic operations, including brackets, follow the same order as arithmetic operations; use index notation for small positive integer powers
- 8Ae3 Construct linear expressions
- **8Ae4** Simplify or transform linear expressions with integer coefficients; collect like terms; multiply a single term over a bracket
- 8Ae5 Derive and use simple formulae, e.g. to convert degrees Celsius (°C) to degrees Fahrenheit (°F)
- **8Ae6** Substitute positive and negative integers into formulae, linear expressions and expressions involving small powers, e.g. $3x^2 + 4$ or $2x^3$, including examples that lead to an equation to solve
- **8Ae7** Construct and solve linear equations with integer coefficients (unknown on either or both sides, without or with brackets)

As Sequences, functions and graphs

- **8As1** Generate terms of a linear sequence using term-to-term and position-to-term rules; find term-to-term and position-to-term rules of sequences, including spatial patterns
- **8As2** Use a linear expression to describe the *n*th term of a simple arithmetic sequence, justifying its form by referring to the activity or practical context from which it was generated
- 8As3 Express simple functions algebraically and represent them in mappings
- **8As4** Construct tables of values and use all four quadrants to plot the graphs of linear functions, where y is given explicitly in terms of x; recognise that equations of the form y = mx + c correspond to straight-line graphs

G Geometry

Gs Shapes and geometric reasoning

- 8Gs1 Know that if two 2D shapes are congruent, corresponding sides and angles are equal
- 8Gs2 Classify quadrilaterals according to their properties, including diagonal properties
- **8Gs3** Know that the longest side of a right-angled triangle is called the hypotenuse
- 8Gs4 Identify alternate angles and corresponding angles
- 8Gs5 Understand a proof that:
 - the angle sum of a triangle is 180° and that of a quadrilateral is 360°
 - the exterior angle of a triangle is equal to the sum of the two interior opposite angles
- **8Gs6** Solve geometrical problems using properties of angles, of parallel and intersecting lines, and of triangles and special quadrilaterals, explaining reasoning with diagrams and text
- 8Gs7 Draw simple nets of solids, e.g. cuboid, regular tetrahedron, square-based pyramid, triangular prism
- 8Gs8 Identify all the symmetries of 2D shapes
- 8Gs9 Use a straight edge and compasses to construct:
 - the midpoint and perpendicular bisector of a line segment
 - the bisector of an angle
- 8Gs10 Use a ruler and compasses to construct:
 - circles and arcs
 - a triangle, given three sides (SSS)
 - a triangle, given a right angle, hypotenuse and one side (RHS)

Gp Position and movement

- 8Gp1 Find the midpoint of the line segment AB, given the coordinates of points A and B
- **8Gp2** Transform 2D shapes by rotation, reflection and translation, and simple combinations of these transformations
- **8Gp3** Understand and use the language and notation associated with enlargement; enlarge 2D shapes, given a centre of enlargement and a positive integer scale factor
- 8Gp4 Interpret and make simple scale drawings

G Measure

Gl Length, mass and capacity

- 8Ml1 Choose suitable units of measurement to estimate, measure, calculate and solve problems in a range of contexts, including units of mass, length, area, volume or capacity
- **8Ml2** Know that distances in the USA, the UK and some other countries are measured in miles, and that one kilometre is about $\frac{5}{8}$ of a mile

Gt Time and rates of change

8Gt1 • 8Mt1 Draw and interpret graphs in real life contexts involving more than one component, e.g. travel graphs with more than one person

Ga Area, perimeter and volume

- **8Ga1 8Ma1** Know the definition of a circle and the names of its parts; know and use formulae for the circumference and area of a circle
- 8Ga2 8Ma2 Derive and use formulae for the area of a triangle, parallelogram and trapezium; calculate areas of compound 2D shapes, and lengths, surface areas and volumes of cuboids
- 8Ga3 8Ma3 Use simple nets of solids to work out their surface areas

D Handling data

Dc Planning and collecting data

- **8Dc1** Identify and collect data to answer a question; select the method of collection, sample size and degree of accuracy needed for measurements
- 8Dc2 Know the difference between discrete and continuous data
- 8Dc3 Construct and use:
 - frequency tables with given equal class intervals to gather continuous data
 - two-way tables to record discrete data

Dp Processing and presenting data

- **8Dp1** Calculate statistics for sets of discrete and continuous data; recognise when to use the range, mean, median and mode and, for grouped data, the modal class
- **8Dp2** Draw, and interpret:
 - frequency diagrams for discrete and continuous data
 - pie charts
 - simple line graphs for time series
 - stem-and-leaf diagrams

Di Interpreting and discussing results

- **8Di1** Interpret tables, graphs and diagrams for discrete and continuous data, and draw conclusions, relating statistics and findings to the original question
- 8Di2 Compare two distributions, using the range and one or more of the mode, median and mean
- 8Di3 Compare proportions in two pie charts that represent different totals

Db Probability

- **8Db1** Know that if the probability of an event occurring is p, then the probability of it not occurring is 1-p
- **8Db2** Find probabilities based on equally likely outcomes in practical contexts
- **8Db3** Find and list systematically all possible mutually exclusive outcomes for single events and for two successive events
- 8Db4 Compare estimated experimental probabilities with theoretical probabilities, recognising that:
 - when experiments are repeated different outcomes may result
 - increasing the number of times an experiment is repeated generally leads to better estimates of probability

Problem solving

Using techniques and skills in solving mathematical problems

- **8Pt1** Calculate accurately, choosing operations and mental or written methods appropriate to the numbers and context
- 8Pt2 Use the order of operations, including brackets, with more complex calculations
- 8Pt3 Manipulate numbers, algebraic expressions and equations, and apply routine algorithms
- 8Pt4 Understand everyday measurement systems, using them to estimate, measure and calculate
- 8Pt5 Recognise and use spatial relationships in two and three dimensions
- 8Pt6 Draw accurate mathematical diagrams, graphs and constructions
- 8Pt7 Estimate, approximate and check working
- **8Pt8** Solve word problems involving calculations with whole numbers, fractions, percentages, decimals, money or measures, including multi-step problems

Using understanding and strategies in solving problems

- **8Ps1** Identify the mathematical features of a context or problem; try out and compare mathematical representations using accurate notation
- 8Ps2 Conjecture and generalise, identifying exceptional cases or counter-examples
- 8Ps3 Use logical argument to interpret the mathematics in a context or to establish the truth of a statement
- 8Ps4 Give accurate solutions appropriate to the context or problem
- 8Ps5 Record and compare reasoning, solutions and conclusions
- 8Ps6 Refine approaches and findings on the basis of discussions with others